Gen. Phys. II Exam 5 - Chs. 30,31,32 - Atomic & Nuclear Physics May. 8, 2018
Rec. Time Name
For full credit, make your work clear. Show formulas used, essential steps, and results with correct units and significant figures. Points shown in parenthesis. For TF and MC, choose the <i>best</i> answer.
OpenStax Ch. 30 - Atomic Physics.
1. (3) The first truly <i>direct</i> evidence of atoms, discovered in 1827 and explained in one of Einstein's 1905 papers, wa
a. Brownian motion. b. Dalton's Law. c. cathode rays. d. kinetic theory.
2. (3) The scientist who is credited with first measuring the charge to mass ratio of electrons (or cathode rays) was
a. Dmitri Mendeleev. b. Ernest Rutherford. c. J.J. Thomson. d. Amedeo Avogadro.
3. (3) Father of nuclear physics Ernest Rutherford discovered the nucleus of gold atoms by bombarding them with
a. electrons. b. protons. c. neutral hydrogen atoms. d. doubly-charged helium nuclei.
Decide whether these statements about the Bohr atomic model are true or false.
4. (2) T F Bohr's model applies only to hydrogen atoms or one-electron ions
5. (2) $\mathbf{T} \mathbf{F}$ Bohr's model explains the similarities between emission and absorption spectra.
6. (2) $\mathbf{T} \mathbf{F}$ Bohr's model predicts a continuous spectrum of emitted light from atoms.
7. (2) T F The de Broglie wavelength in the n^{th} state equals the diameter of the electron's orbit divided by n .
8. (12) The arrows on the diagram show some transitions that a hydrogen atom can make between energy levels, according to the Bohr model. Of the transitions shown,
a) (2) Which transitions correspond to emission of radiation by the atom?
b) (2) Which transitions correspond to absorption of radiation by the atom?

c) (2) Which transition is ionization of the atom?

d) (6) For only the transitions shown, calculate the shortest wavelength *emitted*.

 $\begin{array}{c|c}
 n=\infty \\
 n=3 \\
 c \\
 n=2 \\
 d \\
 e \\
 n=1 \\$

The following questions relate to quantum mechanics (beyond the Bohr model) for atoms.

9. (3) How many electrons in an atom can have the pair of quantum numbers, $n = 3, \ell = 1$?

10. (3) How many electrons in an atom can have the set of quantum numbers, $n = 3, \ell = 1, m_{\ell} = 0$?

- 11. (6) The highest atomic subshells for cobalt (Co) in its ground state have the configuration $3d^{7}4s^{2}$.
- a) (2) What is the value of the orbital quantum number l in the 3d subshell?
 a. 0 b. 1 c. 2 d. 3 e. 4
- b) (2) What is the maximum number of electrons that could occupy the 3d subshell?
- c) (2) Which diagram shows how the 3d electron spins line up (m_s values) in the ground state of cobalt? a. $\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow$ b. $\uparrow\uparrow\uparrow\uparrow\uparrow\uparrow\downarrow\downarrow\downarrow$ c. $\uparrow\uparrow\uparrow\uparrow\uparrow\downarrow\downarrow\downarrow\downarrow$ d. $\uparrow\uparrow\uparrow\uparrow\uparrow\downarrow\downarrow\downarrow\downarrow\downarrow$
- 12. (3) For any atom, which of these electron configurations is not allowed? Check all that apply. a. $1s^22s^22p^3$ b. $1s^22s^23p^3$ c. $1s^22s^22d^3$ d. $1s^22s^12p^1$ e. $1s^22s^12p^7$

13. (3) Into how many different energy levels is the 3d subshell split when a magnetic field is applied ("Zeeman effect")?

a. 2 b. 3 c. 4 d. 5 e. 7 f. 10 g. 14

14. (3) Which of the following outer subshell configurations would correspond to a noble gas? Check all that apply.
a. 2s²
b. 2p²
c. 2p⁵
d. 4p⁶
e. 3d¹⁰

OpenStax Ch. 31 - Radioactivity & Nuclear Physics.

Name

1. (2) Nuclear isotopes are

a. nuclei with the same number of protons but different numbers of neutrons.

b. nuclei with the same number of nucleons but different numbers of neutrons.

c. nuclei with the same number of neutrons but different numbers of protons.

2. (2) For a nuclear decay to take place *spontaneously* (like alpha, beta or gamma decays),

a. the mass of the products must be greater than the mass of the parent nucleus.

b. the mass of the products must be less than the mass of the parent nucleus.

c. the mass of the products must be equal to the mass of the parent nucleus.

3. (2) Carbon-14 forms naturally in Earth's atmosphere due to a nuclear transmution of which element X, according to the reaction, $n+X \rightarrow {}^{14}_{6}C + p$?

a. oxygen (O) b. nitrogen (N) c. helium (He) d. hydrogen (H)

4. (3) A ⁵⁶₂₆Fe (iron) nucleus contains _____ protons and _____ neutrons and _____ nucleons.

5. (3) When radon-222 decays by α -emission, what is the daughter nucleus? Give its name, mass number A and atomic number Z.

6. (3) When cobalt-60 decays by γ -emission, what is the daughter nucleus? Give its name, mass number A and atomic number Z.

7. (3) When potassium-40 decays by β^- emission, what is the daughter nucleus? Give its name, mass number A and atomic number Z.

8. (8) Iron $\binom{56}{26}$ Fe) is one of the most strongly bound nuclei. Calculate the binding energy per nucleon for $\frac{56}{26}$ Fe, which has an atomic mass of 55.934942 u. [Make use of this: Hydrogen (i.e., proton+electron) ¹/₁H atomic mass is 1.007825 u, and neutron mass is 1.008665 u.]

9. (8) Phosphorous-32 $\binom{32}{15}$ P) decays by β^- emission with a half-life of 14.262 days. If you start with a pure 1.00 gram sample of P-32, what mass of P-32 remains after 30.0 days?

10. (18) The ratio of carbon-14 to carbon-12 atoms in living things is about 1.3×10^{-12} . Carbon-14 has a half-life of 5730 years and the decay constant is $\lambda = \ln(2)/T_{1/2} = 3.83 \times 10^{-12} \text{ s}^{-1} = 1.21 \times 10^{-4} \text{ year}^{-1}$. 250-grams of carbon in a sample of ancient wood has an activity of 15.0 decays/s.

a) (6) About how many C-14 atoms were present in this wood sample when the tree died?

b) (6) Based on its activity, about how many C-14 atoms are now present in the wood sample?

c) (6) How old is the wood sample, in years (i.e., the time passed since the tree died)?

OpenStax Ch. 32 - Applications of Nuclear Physics. Name
1. (3) Ionizing radiation emanating from nuclei is dangerous to the human body because
a. It transforms one element into another element.b. It causes molecules to emit light.c. It breaks chemical bonds, especially in DNA.b. It causes atoms to recoil from the emission.
2. (3) Which of the following would be considered ionizing radiation? Check all that apply.
a. 4 MeV α particles. b. 4 keV β^- particles c. 4 keV γ rays. d. 4 eV photons.
3. (3) Which type of radiation has the largest range (or is the most deeply penetrating)?a. alpha particles b. beta particles. c. gamma rays.
4. (3) RBE (relative biological effectiveness or quality factor) accounts for the fact that a. lighter radiation particles cause more damage. c. damage that is spread out is harder to repair. d. charged radiation particles cause more damage. d. charged radiation particles cause more damage.
 5. (3) For the same energy particles inside the body, which type of radiation produces the most localized damage that is hardest for the body to repair? a. α-particles. b. β-particles. γ-rays. d. slow neutrons.
 6. (2) T F The annual effective dose due to radon gas is a negligible part of all background radiation. 7. (2) T F A radiation exposure of 20 sieverts in one sudden event is likely to be fatal.
8. (2) Uranium that is enriched for use in reactors is high in a. iron-56.b. uranium-92.c. uranium-235.d. uranium-238.
9. (2) Fission of heavy elements can become a chain reaction because fission releases a. α -particles. b. β -particles. c. γ -rays. d. protons. e. neutrons.

10. (8) For a 70.0-kg person, the background activity due to carbon-14 within the body is about 3.5 kBq. Each β^- from a carbon-14 decay has an energy of 156.5 keV, and RBE = 1. Calculate the annual effective radiation dose (or dose equivalent, in mSv) if all of the β^- are absorbed within the body.

11. (4) Consider the reaction, ${}^{2}_{1}\text{H} + {}^{3}_{1}\text{H} \rightarrow {}^{4}_{2}\text{He} + X$, where X is some unknown.

- a) (2) The type of reaction is a. α -decay. b. β -decay. c. γ -decay. d. fusion. e. fission.
- b) (2) What is X?
- 12. (4) Consider the reaction, $n + \frac{235}{92}U \rightarrow \frac{137}{56}Ba + \frac{84}{36}Kr + X$, where X is some unknown.
- a) (2) The type of reaction is a. α -decay. b. β -decay. c. γ -decay. d. fusion. e. fission.
- b) (2) What is X?
- 13. (12) The deuterium fusion reaction, ${}^{2}_{1}\text{H} + {}^{2}_{1}\text{H} \rightarrow {}^{3}_{2}\text{He} + n$, releases an energy output of Q = 3.27 MeV. Suppose a nuclear reactor is designed to use this reaction, and it consumes 0.250 μ g of deuterium per second.

a) (6) How many of the given reactions are taking place per second?

b) (6) What is the power output of the reactor, in watts (or kW or MW, etc., if more convenient)?

<u>Prefixes</u>

 $a=10^{-18}$, f=10⁻¹⁵, p=10⁻¹², n=10⁻⁹, $\mu = 10^{-6}$, m=10⁻³, c=10⁻², k=10³, M=10⁶, G=10⁹, T=10¹², P=10¹⁵

Physical Constants

$$\begin{split} &k = 1/4\pi\epsilon_0 = 8.988 \ \text{GNm}^2/\text{C}^2 \ (\text{Coulomb's Law}) \\ &e = 1.602 \times 10^{-19} \ \text{C} \ (\text{proton charge}) \\ &c = 3.00 \times 10^8 \ \text{m/s} \ (\text{speed of light}) \\ &m_e = 9.1094 \times 10^{-31} \ \text{kg} \ (\text{electron mass}) \\ &m_n = 1.67493 \times 10^{-27} \ \text{kg} = \ (\text{neutron mass}) \\ &h = 6.62607 \times 10^{-34} \ \text{J} \cdot \text{s} \ (\text{Planck's constant}) \end{split}$$

Units

$$\begin{split} N_A &= 6.02 \times 10^{23} / \text{mole (Avogadro's } \#) \\ 1.0 \text{ eV} &= 1.602 \times 10^{-19} \text{ J (electron-volt)} \\ 1 \text{ F} &= 1 \text{ C/V} = 1 \text{ farad} = 1 \text{ C}^2 / \text{J} \\ 1 \text{ A} &= 1 \text{ C/s} = 1 \text{ ampere} = 1 \text{ coulomb/second} \\ 1 \text{ T} &= 1 \text{ N/A} \cdot \text{m} = 1 \text{ tesla} = 1 \text{ newton/ampere-meter} \\ 1 \text{ Bq} &= 1 \text{ becquerel} = 1 \text{ decay/s} \end{split}$$

Some Masses (for neutral atoms)

electron = ${}^0_{-1}$ e = 0.00054858 u = 0.51100 MeV/c² neutron = 1_0 n = n = 1.008665 u = 939.57 MeV/c² deuterium = 2_1 H = d = 2.014102 u helium-3 = 3_2 He = 3.016029 u

OpenStax Chapter 30 Equations - Atomic Physics

Bohr Model:

 $hf = E_n - E_{n'} \quad \text{(quantum jump)}$ $r_n = \frac{n^2}{Z}r_1 \quad \text{(Bohr radii)}$ $E_n = -(13.6 \text{ eV})\frac{Z^2}{n^2} \quad \text{(Bohr energies)}$ $n = 1, 2, 3, \dots \quad \text{(Bohr's quantum number)}$

Quantum numbers for atoms:

principle quantum number n = 0, 1, 2, 3...orbital quantum number l = 0, 1, 2...(n - 1)magnetic quantum number $m_l = -l$ to +lspin quantum number $m_s = -\frac{1}{2}, +\frac{1}{2}$ shell $(2n^2 \text{ states})$ means a value of (n) is given. orbital (2 states) means particular (n, l, m_l) are given. $\begin{aligned} \epsilon_0 &= 1/4\pi k = 8.854 \text{ pF/m (permittivity of space)} \\ \mu_0 &= 4\pi \times 10^{-7} \text{ T·m/A (permeability of space)} \\ c &= 2.99792458 \times 10^8 \text{ m/s (exact value in vacuum)} \\ m_p &= 1.67262 \times 10^{-27} \text{ kg (proton mass)} \\ hc &= 1239.84 \text{ eV·nm (photon energy } = hc/\lambda) \\ \hbar &= 1.05457 \times 10^{-34} \text{ J·s (Planck's constant/2\pi)} \end{aligned}$

1 u = 1 g/ N_A = 1.6605 × 10⁻²⁷ kg = 931.5 MeV/c² (mass unit) 1 V = 1 J/C = 1 volt = 1 joule/coulomb 1 H = 1 V·s/A = 1 henry = 1 J/A² 1 Ω = 1 V/A = 1 ohm = 1 J·s/C² 1 G = 10⁻⁴ T = 1 gauss = 10⁻⁴ tesla 1 Ci = 1 curie = 3.70 × 10¹⁰ decays/s = 37.0 GBq

proton = ${}^{1}_{1}$ p = p =1.007276 u = 938.27 MeV/c² hydrogen = ${}^{1}_{1}$ H = 1.007825 u = 938.78 MeV/c² tritium = ${}^{3}_{1}$ H = t = 3.016049 u helium-4 = ${}^{4}_{2}$ He = α = 4.002603 u

$$\begin{split} L &= mvr = n\frac{h}{2\pi} \quad \text{(Bohr's quantization)} \\ r_1 &= \frac{h^2}{4\pi^2 m k e^2} = 52.9 \text{ pm } \quad (1^{\text{st}} \text{ Bohr radius}) \\ E_n &= \frac{1}{2}mv^2 - \frac{kZe^2}{r_n} \quad \text{(total energy)} \\ E &= hc/\lambda = (1240 \text{ eV} \cdot \text{nm})/\lambda \text{ (photons)} \end{split}$$

$$\begin{split} E_n &= -(13.6 \text{ eV})/n^2 \quad (\text{energy of hydrogen states}) \\ L &= \sqrt{l(l+1)} \ \hbar \quad (\text{angular momentum magnitude}) \\ L_z &= m_l \hbar \quad (z\text{-component of } \vec{L}) \\ S_z &= m_s \hbar \quad (z\text{-comp., spin angular momentum}) \\ sub-shell \left[2(2\ell+1) \text{ states} \right] \text{ means values of } (n,l) \text{ are given.} \\ state \text{ means particular } (n,l,m_l,m_s) \text{ are given.} \end{split}$$

l=0,1,2,3,4,5,6... are indicated with respective letters: s, p, d, f, g, h,...

Pauli exclusion principle: No two electrons in an atom can occupy the same quantum state. Subshells in order of increasing energy: 1s, 2s, 2p, 3s, 3p, 4s, 3d, 4p, 5s, 4d, 5p, 6s, 4f, 5d, 6p, 7s, 5f, 6d, 7p (They fill in order of increasing n + l, or increasing n if there is a tie.)

Nuclides:

A = N + Z, (mass, neutron, proton numbers)	$r = (1.2 \text{ fm}) A^{1/3}$ (nuclear radius)
$\Delta E = [(\text{mass of parts}) - (\text{mass of nuclide})]c^2$	$\leftarrow \text{(binding energy)}$
$Q = [M_{\rm parent} - M_{\rm products}]c^2$	\leftarrow (disintegration energy)
$1 \text{ u} = 1 \text{ gram} / 6.02 \times 10^{23}$ (atomic mass unit)	1 u · $c^2 = 931.5$ MeV (energy unit)
Half-life $T_{1/2}$ and decay constant λ	
$N = N_0 e^{-\lambda t}$ (decay of parent nuclei)	$N = N_0 \left(\frac{1}{2}\right)^{t/T_{1/2}} \text{(decay by half-lives)}$
$t = \frac{-1}{\lambda} \ln(N/N_0)$ (time when N nuclei remain)	$\mathcal{A} = \left \frac{\Delta N}{\Delta t}\right = N\lambda$ (radio-activity)
$\lambda T_{\frac{1}{2}} = \ln 2$ (decay constant, half-life)	$M = Nm = mass = (\# of nuclei) \times (nuclear mass)$
$\#({}^{14}_{6}C)/\#({}^{12}_{6}C) = 1.3 \times 10^{-12}$ (live carbon ratio)	1 year = 3.156×10^7 seconds

OpenStax Chapter 32 Equations - Applications of Nuclear Physics

Radiation doses:	
absorbed dose = energy absorbed / mass affected	\leftarrow SI unit = 1 gray = 1 Gy = 1 J/kg = 100 rad.
effective dose = absorbed dose \times RBE	\leftarrow SI unit = 1 sievert = 1 Sv = 1 J/kg = 100 rem.
RBE = relative biological effectiveness	RBE = QF = quality factor (units = Sv/Gy).
radiation: γ -rays slow β 's fast β 's slow neutrons	fast neutrons protons α 's heavy ions

10

2 - 5

Reactions:

RBE =

 $Q = [M_{\text{reactants}} - M_{\text{products}}]c^2 \quad \text{(reaction energy)}$ $Q > 0 \quad (Q = \text{mass converted to energy})$

1.7

Q < 0 (|Q| = threshold energy)

10

10 - 20

10 - 20

Energy, power and mass in nuclear reactors:

1

$E = mc^2$	(Einstein's mass-energy equivalence)	
E = NQ	$[energy= (\# of reactions) \times (reaction energy)]$	
M = Nm	$[mass used = (\# of reactions) \times (reaction mass)]$	
$E_{\rm out} = eE_{\rm in}$	$[output energy = (efficiency) \times (input energy)]$	

1

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P = E/t \quad \text{(power)}
1 u · c^2 = 931.5 \text{ MeV}
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Group Group Group Group Group Group **Periodic Table of the Elements**[§] 2.00 anon U

I	II				Tri	ansition]	Elements					III	IV	V	VI	VII	IIIA
H 1																	He 2
1.00794																	4.002602
1s ¹	- - -																152
Li 3	Be 4			Sym	bol - C	1 17	- Atomic	Number				B 5	C. 6	L N	0 8	F 9	Ne 10
6.941	9.012182		At	omic Ma	SS [§] - 35	.4527					×	10.811	12.0107	14.00674	15.9994	18.9984032	20.1797
251	2.52	i a'			3p	5	- Electro	n Config	uration			2p ¹	2p ²	2p ³	2p ⁴	2p ⁵	2p ⁶
Na 11	Mg 12				qsV		(outer	shells on	y)		2	Al 13	Si 14	P 15	S 16	CI 17	Ar 18
22.989770	24.3050	0 0										26.981538	28.0855	30.973761	32.066	35.4527	39.948
351	352				tani tani		- 1	001	280	200	14. 04.	3p ^r	3p ²	3p ³	3p4	3p ⁵	3p6
K 19	Ca 20	Sc 21	Ti 22	V 23	Cr 24	Mn 25	Fe 26	Co 27	Ni 28	Cu 29	Zn 30	Ga 31	Ge 32	As 33	Se 34	Br 35	Kr 36
39.0983	40.078	44.955910	47.867	-50.9415	51.9961	54.938049	55.845	58.933200	58.6934	63.546	65.39	69.723	72.61	74.92160	78.96	79.904	83.80
451	452	3d1452	3d ² 4s ²	3d ³ 4s ²	3d ⁵ 4s ¹	3d5452	346452	3d ⁷ 4s ²	3d ⁸ 4s ²	3d104s1	3d ¹⁰ 4s ²	4p ¹	4p ²	4p ³	4p ⁴	4p ⁵	4p6
Rb 37	Sr 38	Y 39	Zr 40	Nb 41	Mo 42	Tc 43	Ru 44	Rh 45	Pd 46	Ag 47	Cd 48	In 49	Sn 50	Sb 51	Te 52	I 53	Xe 54
85.4678	87.62	88.90585	91.224	92.90638	95.94	(86)	101.07	102.90550	106.42	107.8682	112.411	114.818	118.710	121.760	127.60	126.90447	131.29
12 281	5.82	4d ¹ 5s ²	4d ² 5s ²	4d ⁴ 5s ¹	4d55s1	4d ⁵ 5s ²	4d ⁰ 5s ¹	4d ⁸ 5s ¹	4d ¹⁰ 5s ⁰	4d ¹⁰ 5s ¹	4d ¹⁰ 5s ²	5p ¹	5p ²	5p ³	5p4	5p ⁵	5p ⁶
Cs 55	Ba 56	57-71 [†]	Hf 72	Ta 73	W 74	Re 75	Os 76	Ir 77	Pt 78	Au 79	Hg 80	TI 81	Pb 82	Bi 83	Po 84	At 85	Rn 86
132.90545	137.327		178.49	180.9479	183.84	186.207	190.23	192.217	195.078	196.96655	200.59	204.3833	207.2	208.98038	(209)	(210)	(222)
6s ¹	6s ²		5d ² 6s ²	5d ³ 6s ²	5d ⁴ 6s ²	545652	5d66s2	5d ⁰ 6s ²	5d ⁹ 6s ¹	5d10651	5d ¹⁰ 6s ²	6p ¹	6p ²	6p ³	6p ⁴	6p ⁵	6p ⁶
Fr 87	Ra 88	89-103	Rf 104	Db 105	Sg 106	Bh 107	Hs 108	Mt 109	Ds 110	111	. 112						
(223)	(226)	1	(261)	(262)	(266)	(264)	(269)	(268)	(271)	(272)	(277)						
751	752	2	6d ² 7s ²	6d ⁹ 7s ²	6d ⁴ 7s ² 2.	6d ⁵ 75 ²	6d ⁶ 75 ²	6d ⁷ 75 ²	152699	6d ¹⁰ 75 ¹	6d ¹⁰⁷⁵²						
							ž	с	101	10 10 10 10 10	101 491) 702	iar iar	501. 501.	ter Kern	101 1 101 1 101 1		2
			La 57	Ce 58	Pr 59	09 PN	Pm 61	Sm 62	Eu 63	Gd 64	Tb 65	Dy 66	Ho 67	Er 68	Tm 69	Yb 70	Lu 71
[†] L.	anthanid	e Series	138.9055	140.115	140.90765	144.24	(145)	150.36	151.964	157.25	158.92534	162.50	164.93032	167.26	168.93421	173.04	174.967
			5d ¹ 6s ²	4f15d1652	4f35d06s2	4f ⁴ 5d ⁰ 6s ²	4f55d ⁰ 6s ²	4f65d06s2	4f^5d06s2	4f"5d"652	4f95d06s2	4f105d06s2	4f115d06s2	4f125d06s2	4f135d06s2	4f145d06s2	4f ¹⁴ 5d ¹ 6s ²

[§] Atomic mass values averaged over isotopes in the percentages they occur on Earth's surface. For unstable elements, mass of the longest-lived known isotope is given in parentheses. 2003 revisions. (See also Appendix B.)

5f26d17s2 5f36d17s2 5f36d17s2 5f46d17s2 5f96d07s2 5f96d17s2 5f96d07s2 5f96d07s2 5f16d07s2 5f16d07s2 5f16d07s2 5f156d07s2 5f136d07s2 5f146d07s2 5f146d07s2 5f146d07s2

(262)

(259)

(258)

(257)

(252)

(251)

(247)

(247)

(243)

(244)

(7237)

238.0289

(1231)

(227.02775) 232.0381 6d²7s²

[‡]Actinide Series

6d¹75²

Ac 89 Th 90 Pa 91 U 92 Np 93 Pu 94 Am 95 Cm 96 Bk 97 Cf 98 Es 99 Fm 100 Md 101 No 102 Lr 103